Dynamics of Exchange at Gas-Zeolite Interfaces I: Pure Component \( n \)-Butane and Isobutane

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We present the results of Molecular Dynamics and Monte Carlo simulations of \( n \)-butane and isobutane in silicalite. We begin with a comparison of the bulk adsorption and diffusion properties for two different parameterizations of the interaction potential between the hydrocarbon species, both of which have been shown to reproduce experimental gas–liquid coexistence curves. We examine diffusion as a function of the loading of the zeolite, as well as the temperature dependence of the diffusion constant at loading and for infinite dilution. Both force fields give accurate descriptions of bulk properties. We continue with simulations in which interfaces are formed between single component gases and the zeolite. After reaching equilibrium, we examine the dynamics of exchange between the bulk gas and the zeolite. In particular, we examine the average time spent in the adsorption layer by molecules as they enter the zeolite from the gas in an attempt to probe the microscopic origins of the surface barrier. The microscopic barrier is found to be insignificant for experimental systems. Finally, we calculate the permeability of the zeolite for \( n \)-butane and isobutane as a function of pressure. Our results underestimate the experimental results by an order of magnitude, indicating a strong effect from the surface barrier in these simulations. Our simulations are performed for a number of different gas temperatures and pressures, covering a wide range of state points.

I. Introduction

Zeolites are microporous materials that are ideally suited to a number of different industrial applications such as catalytic cracking or hydroisomerization of hydrocarbon molecules as well as ion exchange in desiccant or purification applications. Zeolites with medium pore sizes, such as silicalite (structure type MFI), are additionally useful for separations processes, as their openings are approximately the same size as the kinetic diameter of many small molecules. As such, the utility of any given zeolite in a separations application is strongly dependent on the preferential adsorption, as well as the relative diffusivities of the sorbed species.

There exists a large body of theoretical\textsuperscript{2–6} and experimental\textsuperscript{7–14} work that investigates the diffusion properties of small alkanes in zeolites. Simulations are generally performed with either Molecular Dynamics (MD) or Monte Carlo (MC) methods,\textsuperscript{15} both of which give calculated diffusivities that agree well with each other, although the MC methods, not having a true time dependence, rely on transition state theory for rate constants. The experimental situation is much less clear. Experimental diffusion constants can be measured through both microscopic and macroscopic methods, with the calculated diffusivities differing by an order of magnitude or more between the two methods. Although macroscopic studies measure the diffusion of the molecules indirectly, as in supported membrane studies where the diffusion is calculated from the permeation flux, the microscopic measurements directly follow the mean-squared displacement of individual molecules. This is the same method that is traditionally used in simulations, and it is for this reason that simulations tend to agree more with microscopic diffusion studies rather than macroscopic. It has been suggested that the difference between the macroscopic and the microscopic measurements lies in the improper assumption of Fickian diffusion in the former\textsuperscript{16} or the difference between the diffusion of gas-phase and adsorbed components,\textsuperscript{17} but this discussion lies outside the scope of this paper. With the above in mind, when both macroscopic and microscopic measurements are available for comparison with our simulations, we only use the microscopic measurements.

Simulations of molecular adsorption on zeolites have traditionally been MC studies of adsorption isotherms.\textsuperscript{18–22} Although MC methods are much more efficient for computing equilibrium properties of the gas/zeolite system than MD, MC is not well suited for calculating time dependent properties. We are primarily interested in the dynamics of exchange between the gas and adsorbed phases through direct analysis of molecular trajectories which are not available from MC interface simulations. In fact, although our MC studies include a gas phase in the simulation, most do not, instead relying on parameterized equations of state that equate a calculated chemical potential with a gas pressure.\textsuperscript{22} It is for these reasons that we have focused our transport studies on MD simulations. We have verified that MD simulations equilibrate to the state points as given by the
adsorption isotherms from MC (see below). With the demonstrated success of MD simulations in both the gas and the zeolite, as well as at the interface (i.e., adsorption isotherms), we feel that the specifics of molecular exchange between the gas and the zeolite are equally well represented, and elucidate the dynamics of a process that cannot presently be investigated experimentally.

For this work, we restrict ourselves to \( n \)-butane (hereafter butane) and isobutane. The use of these small molecules avoids the computational burden associated with longer molecules, while still allowing us to compare fast and slow diffusing species.

The remainder of the paper is arranged as follows: In section II, we present the details of our simulation methodology, including descriptions of the parameter sets used. We continue in section III with the results of our simulations of bulk zeolite crystals. These include adsorption isotherms and diffusion studies. Our interface simulations are presented in IV, where we examine the exchange dynamics for systems in equilibrium. We present nonequilibrium permeation studies, in which a concentration gradient appears on either side of the zeolite membrane in section V. We conclude and discuss our future work in section VI.

II. Simulation Details

We perform MD simulations of butane and isobutane using an united atom (UA) representation for the \( \text{CH}_5 \) groups, in which each group is treated as a single pseudo-atom. For the diffusion and interface simulations we used two different simulation codes, one of which constrained all C–C bond lengths to 1.54 Å using the RATTLE algorithm,\(^{15} \) whereas the other used a harmonic potential between UAs with a spring constant of 452 900 K/Å\(^2\).\(^{16} \) The simulations with the constrained bonds used a 5 fs time step and a Langevin thermostat.\(^{15} \) Those with the harmonic potential used a multiple time step \( r \)RESPA algorithm\(^{24} \) with a 1.25 fs time step for the bonds, a 2.5 fs time step for the angles, and a 5 fs time step for the interaction between nonbonded \( \text{CH}_5 \) UAs. Temperature control in these simulations used a Nosé–Hoover thermostat. The former simulations were run with the same code as in our previous work,\(^{25,26} \) whereas the latter were run with the large-scale parallel MD code LAMMPS.\(^{27} \) We have verified that these two different approaches equilibrate to the same points on the isotherms. We have found slight differences in the exchange dynamics between the two codes when run as described above. These differences, however, disappeared when both codes were implemented with a Langevin thermostat. For technical reasons, the multitime step \( r \)RESPA algorithm is not presently implemented with Langevin dynamics. Hence, to compare exchange dynamics from Nosé–Hoover and Langevin thermostats, simulations were run with both codes using a single time step of 1.25 fs. A Nosé–Hoover thermostat is essentially a velocity rescaling scheme, which adds no randomness to the system, velocities of all particles are scaled so as to make the kinetic temperature match the prescribed temperature. This type of thermostat is most applicable in dense systems, such as liquids, where frequent molecular collisions serve to randomize velocities. The Langevin thermostat, on the other hand, couples the particles to a heat bath via a random force and viscous damping, which are coupled through the fluctuation–dissipation theorem. The Langevin thermostat is most appropriate for our interface simulations, as it simulates both collisions with a carrier gas as well as the effect of a vibrating crystal lattice for molecules adsorbed inside the zeolite. It is for these reasons that most of our simulations are performed with a Langevin thermostat, especially where dynamical information is desired.

Both codes include three body bending \( V_b \) and four body torsion \( V_t \) terms\(^{15} \) of the forms below.

\[
V_b(\theta) = \frac{k_b}{2}(\theta - \theta_b)^2 \tag{1}
\]

\[
V_t(\phi) = \sum_i a_i \cos^6(\phi) \tag{2}
\]

where \( k_b \) is the angular spring constant, \( \theta \) (\( \theta_b \)) is the (equilibrium) angle between three neighboring atoms, and \( \phi \) is the torsional angle as described in ref 15. All nonbonded interactions are governed by a 12–6 cut and shifted Lennard–Jones (LJ) interaction

\[
V_{LJ}(r) = 4\epsilon \left[ \left( \frac{\sigma}{r} \right)^{12} - \left( \frac{\sigma}{r} \right)^{6} \right] \tag{3}
\]

with a cutoff of \( r_c = 10 \) Å unless otherwise indicated. For the adsorption isotherms in section IIIA we also present results for larger values of the cutoff, \( r_c = 14 \) and 18 Å. We use two different parametrizations for the LJ interactions, both developed by Siepmann and co-workers to accurately predict vapor–liquid coexistence curves for linear and branched alkanes of various lengths\(^{28–33} \) (see Tables 1 and 2). We refer to these parameterizations as mSKS (modified Siepmann, Karaborni, Smit)\(^{28–31} \) and TraPPE (Transferable Potentials for Phase Equilibria),\(^{32,33} \) respectively. In both force fields, methyl, methylene, and methine groups are described by a single set of parameters regardless of their neighbors. Note that although this is the prescription for the TraPPE force field, the original SKS force field had a methyl group whose parameters depended upon its neighbors. To reduce confusion we refer to our SKS force field (i.e., with constant methyl group parameters) as mSKS.

The reason for using two different potential sets is 2-fold. First, although the TraPPE force field reproduces the experimental vapor–liquid coexistence curves better than SKS, it is unknown how the two sets compare for dynamical measurements, such as diffusion constants. Second, our previous work on the diffusion of long linear and branched alkanes used the mSKS potential set,\(^{25,26} \) and this study can help to understand how the results from that work relate to the new potential set. The zeolite structure in our simulation is taken from the database contained in the Insight II software from Molecular Simulations, Inc.\(^{34} \) and is assumed to be rigid. The LJ interaction

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between the atoms of the zeolite and the UAs of the alkanes is taken from the work of June et al., with a slight modification. In the original work, all UAs (i.e., CH$_3$ and CH$_2$) were treated as identical units. For this work, we have normalized this interaction to decane in order to arrive at separate parameters for the different UAs, as described previously. These parameters are not optimized for diffusion or adsorption and thus perform adequately at best, particularly for isobutane, but this is not of concern as our primary purpose is to compare the dynamics within the given alkane models, using the same alkane/zeolite interaction.

Isotherms were computed using a combination of coupled—decoupled configurational-bias MC simulations and the isobaric—isothermal version of the Gibbs ensemble. This formulation is useful for comparison to experimental isotherms in which the temperature and pressure of the gas are held constant. One simulation box contained 12 unit cells of silicalite and was kept at a constant volume, whereas the other simulation box exchanged volume with an external pressure bath. The system contained 400 solute molecules which were allowed to exchange between the two simulation boxes. Simulations were run for 10 000 cycles, where each cycle consisted of 400 MC steps. Molecules were chosen at random with a fixed probability of performing a volume move (0.01), molecule exchange (0.19), molecule regrowth (0.2), translation of the center of mass (0.3), and rotation about the center of mass (0.3). The maximum volume, translational, and rotational displacements were automatically adjusted to achieve an acceptance rate of 50%.

For our diffusion studies, our zeolite crystal contained 96 unit cells, four each in the (100) and (001) directions, and six in the (010) direction. Periodic boundary conditions were applied in all directions. For all diffusion studies, guest molecules were inserted along the straight channels of the zeolite and allowed to diffuse at high temperature (e.g., 900 K). The temperature was gradually reduced to the desired temperature for a given run, and the system was then allowed to equilibrate before data were taken. In the dilute limit (i.e., noninteracting sorbate molecules) we simulated 96 molecules, whereas for finite density, the number of molecules ranged from 96 to 768. Our interface runs used the same zeolite crystal as the diffusion studies with the addition of a large (∼100 Å) gas region alongside the (010) crystal face. Because the gas is exposed to the external surface of the zeolite, the true nature of this surface becomes relevant. For example, the surface will likely be reconstructed, and consist of a mixture of undercoordinated and overcoordinated oxygen atoms. As our MD simulations cannot probe the true nature of the surface, we have instead investigated the effects of differing termination by first examining the two extremes of fully coordinated and fully undercoordinated oxygens at the surface. We have further modified the latter surface to include the effects of hydroxylation by changing the LJ interaction of these oxygens. We found no dramatic differences in these simulations and will not discuss them here. Our interface simulations were performed in three stages. The first stage was a gas equilibration run in which a given number of molecules (typically 800–2000) were equilibrated at constant temperature. The simulation box for this stage had periodic boundary condition in the x and z directions, but was confined in the y direction by walls with a 9–3 LJ potential. The x and z box dimensions matched those of the zeolite crystal in the (100) and (001) directions. The spacing between the LJ walls was adjusted to give a desired gas density. After equilibrium was reached, we began the second stage of the simulation, where the LJ walls were removed and the gas was placed alongside the zeolite with periodic boundary conditions in all directions. The gas molecules adsorbed onto the zeolite crystal and an equilibrium state point was reached when the pressure in the gas and the loading of the zeolite matched the adsorption isotherm for the system temperature. We show in Figure 1 a representative snapshots of one of our interface simulations. In Figure 1a, we show a side view of our simulation box, with the butane molecules in the gas, adsorption layer and zeolite colored red, yellow, and light blue, respectively, and the zeolite represented by purple bonds. Figure 1a shows a gas region with a pressure of approximately 5.5 MPa, and the corresponding highly loaded zeolite. In Figure 1b and c we show closeup snapshots of the adsorbed surface layer for dilute and dense gas regions, respectively. Because we specify the system volume V, the number of molecules N, and the temperature T only, the pressure P, and loading that are finally reached cannot be specified in advance, although with careful selection of N for a given T and V, we can come close to any desired point on the isotherm.

The membrane permeation simulations were performed using the parallel grand-canonical (GC) MD code LADERA. Two zeolite membranes were positioned in a simulation box of total length 137.30 Å, oriented so that the straight-channels traversed the membrane, and the sinusoidal channels lay in the plane of the membrane. Each membrane had cross-sectional dimensions of 2 unit cells in the (001) direction and 3 units cells in the (100) direction (approximately 40 Å × 40 Å). The zeolite membranes separated the remaining volume into two gas regions, each approximately 29 Å thick. Periodic boundary conditions were applied in all three directions. Hence, the simulation box represented an infinite set of infinite parallel zeolite membranes separated by gas regions of alternating high and low pressure. A constant chemical potential was maintained within a 15 Å thick region at the center of each gas region. This was done by performing insertions and deletions of gas molecules according to the grand canonical MC algorithm. Using this method, the pressures and densities on the high and low sides were maintained at constant but different values. At the same time, trajectories of all the molecules in the simulation box were followed using a conventional molecular dynamics algorithm, based on the LAMMPS code. As a result, the simulation evolved in time to a condition of steady-state, with a constant net flux of molecules moving from the high-pressure side, through both zeolite membranes, to the low-pressure side. This flux was maintained by a net addition of molecules in the high-pressure control volume and a net removal of molecules in the low-pressure control volume.

For the permeation studies, the zeolite and gas molecule interaction potentials were identical to those described above, with two exceptions. First, the Lennard—Jones interactions were truncated at 10 Å but were not shifted. This has no effect on the permeation of molecules through the zeolite, which is only dependent on the forces, but it is important for the definition of chemical potential. Second, in the MD portion of the calculation, which used the velocity-Verlet algorithm with constant volume and temperature and a time step of 3 fs, the temperature was controlled by velocity rescaling. We have found no difference when we ran the same state points with a Nose—Hoover thermostat. A set of insertion and deletion attempts were performed in the control volumes every 1000 time steps. Each set consisted of 32 attempts in each control volume, with insertions and deletions chosen at random with equal probability.
III. Bulk Properties

Before discussing the dynamics of the gas-zeolite interfaces, we present our results for a bulk zeolite. These include the thermodynamic properties of zeolite adsorption as probed through adsorption isotherms, and diffusion studies in the infinite dilution limit and at finite loading.

A. Thermodynamic Properties. We begin with a comparison of the adsorption isotherms from both potential sets and experiment for both molecules. In Figure 2(a) we show the comparison for \( n \)-butane with the mSKS and TraPPE force fields at 353 K with a cutoff of 10 Å. We have chosen these parameters to match those used in the MD simulations below. We also show in Figure 2a the experimental data from Sun et
al. at the same temperature. The agreement is excellent for the TraPPE force field and fair for mSKS, but quite acceptable, considering that neither parameter set was optimized for adsorption studies.

We show the comparison for isobutane in Figure 2b. The agreement between TraPPE and mSKS is reasonable, but neither force field can accurately reproduce the experimental data. In particular, both force fields fail to exhibit the plateau in the isotherm in the region of 4 molecules/unit cell, and overshoot the maximum filling by nearly a factor of 2. This difficulty in fitting isobutane adsorption has also been seen by Macedonia and Maginn in their work with a consistent-valence force field all-atom method. That work found better agreement with a UA method with parameters that were optimized for zeolite adsorption. The lack of agreement between our calculated and experimental isotherms is a symptom of the hybrid origin of the force fields, and demonstrates the sensitivity of adsorption simulations on the parameterization of large molecules (i.e., those with kinetic diameters close to the pore size). We emphasize that our purpose in this section is to compare our state points with experiment, not to fit them. We are more interested in verifying that our MD interface simulations have converged to the correct state points for a given model, and the isotherms shown in Figure 2 serve that purpose.

In Figure 3a and 3b, we show the MC isotherms for butane and isobutane, respectively, as a function of temperature. For comparison, we also show results from the MD interface runs at 500 K. We stress, however, that while isotherms can be successfully reproduced with the MD simulations, the direct integration of molecular trajectories leads to long equilibration times (in excess of 20 ns for isobutane), and thus extremely long run times. The MC method is much better suited to isotherm calculations, but is unable to give the dynamics of exchange that are the ultimate goal of this work.

The calculated isotherms can be fit well with a simple Langmuir isotherm

\[ q(P) = q_{\text{sat}} \frac{KP}{1 + KP} \]

where \( q(P) \) is the filling of the zeolite, \( q_{\text{sat}} \) is the saturation filling and \( K \) is the Langmuir constant. This has been shown previously by other authors. We show these fits for 500 K in Figure 3a and 3b. The good fits from the Langmuir isotherm suggest that the molecules have preferential adsorption sites within the zeolite. The Langmuir fits begin to fail at lower temperatures and higher pressures, due to the presence of additional adsorption sites that are relatively energetically unfavorable. For example, isobutane is known to preferentially load the intersections between the straight and sinusoidal channels in silicalite due to its large kinetic diameter. At higher pressures, however, the intersections become filled, and the sorbed molecules are forced into the channels of the zeolite. These multiple adsorption sites are taken into account by a double Langmuir fit for isobutane.

To conclude our thermodynamic studies, we investigate the effect of the LJ cutoff on the calculated isotherms. We perform the bulk of our simulations with a 10 Å cutoff, and show below that the effect of the cutoff on dynamic properties, such as the diffusivity at constant loading is small. The effect of the cutoff
on the adsorption isotherms, however, is more severe. The TraPPE force field was originally parameterized using a 14 Å cutoff with the standard analytical tail corrections. Tail corrections are applied with the implicit assumption that the pair−pair correlation function attains a constant value of 1 beyond the cutoff, an assumption that is incorrect inside a zeolite, as demonstrated by Macedonia and Maginn. The behavior of the model for infinite cutoff within a zeolite is therefore unknown. With this in mind, we present in Figure 4 our MC isotherms for butane on silicalite as a function of the cutoff in the potential. The isotherms shift monotonicly to higher fillings at a given pressure as the cutoff is increased. This is to be expected, since a larger cutoff leads to increased attractive energy. In the figure, the isotherms seem to be converging, though still changing, as the cutoff is increased from 14 to 18 Å. It is certainly possible to increase the cutoff until the isotherms converge, but such an exercise is beyond the scope of this work. Rather, we simply point out that the choice of cutoff is a model parameter that affects the calculated thermodynamic properties of any system. In Figure 4, we also show the calculated isotherm with the TraPPE potential as published, i.e., with a 14 Å cutoff and tail corrections. Even with the caveats above, this isotherm seems close to what would be expected for an infinite cutoff.

B. Diffusion Studies. With an understanding of the thermodynamics of sorption, we now move on to the behavior of the molecules within the zeolite. We begin with the calculated diffusion constant \( D \) in the infinite dilution limit. For all our diffusion measurements, we find the mean squared displacement of individual molecules, and calculate the diffusion constant based on the Einstein relation

\[
\langle r^2 \rangle = 6Dt
\]

where \( \langle r^2 \rangle \) is the mean squared displacement and \( t \) is the time. In Figure 5, we show the calculated diffusivities over the temperature range of 400 K to 800 K for both butane and isobutane with the mSKS and TraPPE potential sets. The results for butane show that over the given temperature range the two potential sets perform identically. This result is not surprising given that the parameterization for butane is almost unchanged between the two force fields. Both parameterizations calculate similar activation energies, 1.01 and 0.78 kcal/mol for the mSKS and TraPPE potentials, respectively. These values compare well with experimentally measured activation energies for butane in silicalite, which range from 1 to 3 kcal/mol.

For isobutane, there is a substantial difference in the calculated diffusivities for the two parameter sets at all \( T \). This difference is clearly due to the different treatment of the \( CH \) UA in the two parameter sets. In the mSKS parameterization, the \( CH \) UA has a radius \( \sigma = 3.85 \) Å and well-depth \( \epsilon = 6.4 \times 10^{-2} \) kcal/mol, whereas in the TraPPE parameterization the values are \( \sigma = 4.68 \) Å and \( \epsilon = 1.99 \times 10^{-2} \) kcal/mol. While the difference in \( \sigma \) is perhaps at first the most surprising, and the size comparison between \( CH \) and \( CH_2 \) and \( CH_3 \) for the TraPPE potential is counter-intuitive, we feel that this is not the cause of the differing diffusivities in Figure 5. Although \( \sigma \) is large for the \( CH \) UA, the surrounding \( CH \) UAs effectively shield the \( CH \) group from the zeolite atoms. Instead it is the value of \( \epsilon \), which is smaller by a factor of 3.2 in the TraPPE potential that leads to the higher diffusivity. A smaller well depth necessarily implies less attraction to the walls of the zeolite, and it is this attraction that contributes most strongly to the diffusion constant in the infinite dilution limit. The weaker attraction is, of course, tempered somewhat by the larger value of \( \sigma \), which implies more attraction at a longer distance. Both models do, however, give similar activation energies of 3.12 and 4.34 kcal/mol for TraPPE and mSKS, respectively. These values also compare well with experimentally measured activation energies, which are generally around 5 kcal/mol.

The good agreement with experimental activation energies is somewhat surprising, given that experiments cannot truly be performed at infinite dilution. With this in mind, we have also investigated the diffusivities of butane and isobutane at various loadings of the zeolite cages. In Figure 6 we show the diffusion of butane in silicalite for both potential sets as a function of loading. Again, it is clear that the small differences in the description of butane within the two force fields results in a minimal difference in the calculated diffusivity. In Figure 6, we also include experimental data taken from Heink et al. These data should not be taken as a strict comparison as they were not tabulated and were inferred from a figure. However, the agreement between simulation and experiment is still quite good.

Even better agreement between simulation and experiment is seen in Figure 7 where we show the diffusion of butane in silicalite as a function of \( T \) at a fixed loading of eight molecules per unit cell. As we have found little difference between the mSKS and TraPPE potential sets, we will hereafter restrict our analyses to TraPPE, as it is designed to treat branched and linear molecules in a consistent fashion. The experimental data were again inferred from a Figure in Heink et al., but we still find
excellent agreement between simulation and experiment. It is important to note, however, that in Figure 6 the points for eight molecules per unit cell are already very close, and thus the excellent agreement in Figure 7 is somewhat fortuitous. Had we chosen a different loading, although the activation energy would change only slightly, there would be a constant factor between the simulated and experimental diffusivities at all temperatures. This is clear from a comparison of the activation energies at infinite dilution and finite loading presented here. Also shown in Figure 7 is the calculated diffusivity at this loading and temperature with a cutoff of 14 Å. It is clear from the figure that the large cutoff has no effect on the diffusion constant at this loading. Because this loading is near to the maximum for butane in silicalite, any effect of the cutoff should be large here. We are now fully justified in our use of the smaller cutoff of 10 Å for our diffusion studies.

We conclude our study of diffusion in silicalite with Figure 8 where we show the simulated and experimental diffusivity of isobutane at a variety of temperatures and loadings. The state points for the simulations were chosen to coincide with those used in the experiments of Millot et al. because of the difficulty in finding experimental diffusion studies of isobutane in a temperature range accessible to simulations. We show the temperatures and corresponding loadings for these data in Table 3. The agreement here between simulation and experiment is fair, but we note two important points. First, the error bars on the experiment are quite large (a factor of 3), which can greatly affect the slope of the line in the figure. Second, the experimental data here are from macroscopic membrane experiments, which are well-known to disagree with MD simulations by an order of magnitude or more. With these points in mind, the agreement is quite acceptable.

IV. Interface Studies

A. State Points. Although relative diffusion rates and bulk sorption studies are of interest in separations applications, the tendency of a given species to adsorb preferentially over other species will also play an important role. As an example, we point to the permeation studies of Krishna and van den Broeke. This work has shown that for binary mixtures of methane and butane, the flux is characterized by an initial sharp peak of methane, which quickly dies out and is replaced by a larger steady flux of butane. The authors ascribe the initial methane flux to its higher relative diffusivity. The relative adsorption, however, eventually leads to a higher filling of butane over methane, and then a higher butane output flux. From a practical standpoint, the adsorption properties must be understood first for pure component gases before the inherently more complicated behavior of mixtures is investigated. We discuss here the results of our interface studies for pure gases only, and will present our simulations of mixtures in a future paper.

Though most of the experiments on separations are at or near room temperature, we often found it necessary to work at more elevated temperatures. Accurate interpretations of the dynamics of exchange between the gas and the zeolite require statistics gathered over a large number of actual exchange events. This, in turn, places requirements on the possible densities, and thus pressures, of the gas phase of the simulations. For good statistics, we need to run our simulations at gas pressures on the order of 100 kPa. Lower pressures imply extremely dilute gas regions, while higher pressures lead to fully loaded zeolites. Both these situations make exchange events rare. Pressures around 100 kPa then restrict us to high temperatures. At the lower temperatures often used in the experiments, pressures close to this would result in the zeolite being loaded to capacity and a thick wetting layer on the crystal surface (see Figure 1). At higher temperatures diffusivities of the sorbed species are enhanced, which
greatly reduces the computational burden. This is especially significant in the case of isobutane, which takes millions of time steps just to equilibrate, even at 500 K.

We show the state points of our butane MD simulations in Figure 9, where we also show the vapor liquid coexistence curve (VLCC) for the TraPPE potential with a 10 Å cut and shifted potential. The VLCC for this potential set deviates considerably from the curve for the full TraPPE potential,32 which shows excellent agreement with experiment. The purpose of this figure, however, is not to compare to experiment, but rather to indicate the state points at which our simulations are performed. As is clear from the figure, we have focused on two different systems, a dilute system, which remains to the left of the coexistence curve at nearly all temperatures studied, and a dense system, which undergoes a phase separation as the temperature is lowered below the critical point $T_c$. In Figure 9, it can be seen that the density of the adsorption layer of the dense system does not exactly match the liquid densities of the VLCC below $T_c$. This is primarily due to the definition of the adsorption layer, which is somewhat arbitrary. Small variations in this definition can lead to changes in the reported liquid densities in Figure 9.

In more dilute systems, liquid layers formed during phase separation may be unable to achieve the density that would be reached were an infinite particle bath available. For this reason, we will not include phase separated state points in the bulk of our discussions below.

**B. Simulation Results.** There are many different paths available for probing the dynamics of the exchanges between the gas and the zeolite. For example, one could choose to examine the mean adsorption time of molecules in the zeolite, or the mean time $t_{ads}$ required for a gas molecule to become adsorbed. As these times can essentially be deduced from the diffusivities of the molecules, we have decided not to investigate these properties. Rather, we have chosen to investigate the relationship of the adsorbed surface layer to the exchanges. Our question is posed as follows: given a molecule which is in the gas at time $t_0$, leaves the gas at time $t_g$, and enters the zeolite at some time $t_e$, what is the meantime this molecule spends in the adsorption layer for times $t_e \leq t \leq t_g$? Furthermore, what are the variables that affect this mean time?

The surface residence time has previously been proposed as the microscopic origin of the surface barrier51,52 which leads to discrepancies between diffusion constants as measured by microscopic and macroscopic experimental methods. Vigné-Maeder et al., studied the entrance of Ar and Xe into both MFI and MOR, and found insignificant surface residence times, while Maeder et al., studied the entrance of Ar and Xe into both MFI and MOR, and found insignificant surface residence times, while Ford and Glandt used a simpler system with single Lennard-Jones particles entering slit pores. Both these works considered small systems in the infinite dilution limit only, and the applicability of their results to true experimental systems is unknown. Our present results are, to the best of our knowledge, the first simulations to examine the effects of the surface barrier for dense alkane gases exposed to large zeolite surfaces.

To begin, we show in Figure 10 a center of mass density profile typical of our equilibrated interface simulations for butane. In this figure, the gas region extends from 80 to 184 Å, where the pressure is approximately 1.2 MPa. The small peaks of the adsorption layer can be seen near 82 and 182 Å and are approximately 5 Å thick. The butane molecules can be seen to preferentially load the sinusoidal channels of the zeolite, as reported by other authors.21 The smaller peaks in the zeolite portion of the density profile correspond to the straight channels, which become populated by butane as the gas pressure increases.

A molecule is identified as residing in the gas at some time $t_g$ when its center of mass lies outside the zeolite and the adsorption layer.53 Adsorbed molecules are identified by a similar criterion. As discussed below, the actual thickness of the adsorption layer is not strictly defined, and can affect results quantitatively, though not qualitatively. Consider the case shown in Figure 11. The path shown by the dashed line represents a common trajectory in which a molecule rapidly exchanges between the gas and the adsorption layer before settling into the layer and later entering the zeolite, represented by the solid line $z$. If the adsorption layer is chosen to be at dotted line 1, this molecule would be counted as spending a long time, $t_1$ in
the adsorption layer. However, if the adsorption layer were chosen to be at either dotted line 2 or 3, the exchanges would not be counted, and the value of $t_{\text{ads}}$ would be a much smaller time, $t_2$ or $t_3$.

In Figure 12 we show the distribution of time spent in the adsorption layer, $t_{\text{ads}}$, by molecules entering the zeolite from the gas for the dilute and dense system, representing a pressure range of approximately 1–20 MPa at $T = 500$ K. Note that the distribution in the figure is dramatically different from the overall lifetime of molecules in the adsorption layer, which has an exponential form as shown in the inset. From Figure 12, it is clear that ballistic entry makes up only a small part of the exchange events. A rough calculation indicates that a molecule entering the zeolite ballistically should spend approximately 1 ps in the adsorption layer at 500 K. It is clear from the figure that the bulk of the molecules spend substantially longer than 1 ps in the adsorption layer, and the mean time is, in fact, on the order of 10 ps. It is also clear from the figure that the pressure dependence, and therefore the dependence on zeolite loading, is extremely weak, at least for the pressure range shown in the figure. The distribution is normalized so that the integral under the curve gives one.

We have fit the distribution for $t_{\text{ads}}$ shown in Figure 12 with a simple binomial distribution of the form

$$B_{n,p}(v) = \binom{n}{v} p^v (1-p)^{n-v}$$  \hspace{1cm} (6)

where $B$ is the total probability, $p$ is the probability of success in a single trial, $n$ is the number of trials, and $v$ is the number of successes.\textsuperscript{54} We also show the fits from eq 6 in Figure 12. For these data, the time step was reduced to 1.25 fs with molecular configurations saved every 0.5 ps in order to increase the resolution. As can be seen in the figure, the fits are quite good for a value of $p = 0.33$. The fits are most accurate at small $t_{\text{ads}}$, but begin to underestimate the data at longer times. This effect is primarily due to our choice of the width of the adsorption layer. The choice of the layer width can clearly affect the distributions shown in Figure 12, as shown in Figure 11. However, as this choice is somewhat subjective, rather than attempt to explain the slight differences between the fits and the data, we point out that the fits demonstrate a physically reasonable functional form for the lifetime.

A binomial distribution suggests that there are a number of distinct adsorption sites on the (010) surface of the zeolite, and adsorbed molecules quickly jump from site to site until they either enter the zeolite or return to the gas. We note that the naive interpretation of this distribution, in which hops on the surface are viewed as failures, and the pore entry is considered a success does not lead to a binomial distribution. This is because such a model requires that a single success occurs after all failures, removing the prefactor from eq 6 and changing the distribution. To obtain a binomial distribution, it is necessary to consider that there are at least two distinct adsorption sites on the surface (labeled arbitrarily as successes or failures), and that molecules actually hop among these sites before entering the pore mouth or returning to the gas. We have examined the validity of this conclusion by calculating the density profile of the center of mass of physisorbed molecules, shown in Figure 13(a) and (b) for butane and isobutane, respectively. For these figures, we show a contour plot of the density of physisorbed molecules averaged over the entire production phase of the simulation, with white (black) representing regions of high (low) density. For clarity, we only show a subsection of the total system in the figures. In the figures, it can be seen that there are a number of distinct adsorption sites surrounding the pore mouths that are preferentially occupied by the butane and isobutane molecules. The highest density is seen to be directly over the pore mouth, indicating that the molecules do not snake their way into the zeolite, hugging close to the surface, but rather hop directly into the potential well of the pore mouth. This picture is consistent with Burggraaf,\textsuperscript{55} who showed that when the ratio of the kinetic diameter of the sorbed molecules to the

Figure 12. Time spent in the adsorption layer by butane molecules as they enter the zeolite from the gas. The squares and circles represent $P = 1$ and $\sim 10$ MPa, respectively, whereas the solid and dashed lines are fits of the low and high pressure points, respectively, to a binomial distribution as described in the text. The inset shows the overall lifetime of molecules in the adsorption layer.

Figure 13. Density profile of (a) butane and (b) isobutane molecules in the adsorption layer over the entire simulation at 500 K. The profile is overlayed over the bonds of the unit cell for clarity. There are a number of distinct adsorption sites present on the surface.
pore opening is close to 1, as is the case for butane and isobutane in silicalite, sorbed molecules feel a deep potential well inside the pores, with nearly equal contributions from both walls. It is interesting to note that the distributions for butane and isobutane are identical.

In addition to $t_{ads}$ for molecules entering the zeolite, we have investigated the related distribution for molecules that leave the zeolite and enter the gas. In Figure 14 we show the distribution for $t_{ads}$ for $T = 500$ K and $P = 1200$ kPa for molecules entering the zeolite from the gas (i.e., the same distribution shown in Figure 12) as well as that for molecules leaving the zeolite and entering the gas. The two distributions are identical within statistical error, indicating that ballistic transport is, again, a relatively unfavorable process. This result also suggests that there are different desorption points for molecules entering the gas and the zeolite. As discussed above, from Figure 13, it is clear that molecules entering the zeolite do so by first hopping to an adsorption site directly above a pore mouth. Molecules leaving the zeolite and entering the adsorption layer must first exit a pore via this same site. If this site were also the site for leaving the zeolite and entering the adsorption layer must first to an adsorption site directly above a pore mouth. Molecules entering the zeolite do so by first hopping gas and the zeolite. As discussed above, from Figure 13, it is clear that molecules entering the zeolite do so by first hopping to an adsorption site directly above a pore mouth. Molecules leaving the zeolite and entering the adsorption layer must first exit a pore via this same site. If this site were also the site for desorption into the gas, then the probability for ballistic exit (or very small $t_{ads}$) in Figure 14 would dominate. This is not the case. Rather, molecules leaving the zeolite enter the adsorption layer via the adsorption site directly above the pore mouth, and then hop from adsorption site to adsorption site until the preferred site for desorption into the gas is reached. This, coupled with the lack of variation of $t_{ads}$ over a wide pressure range, indicates that even for extremely low back-pressures, such as those realized in membrane permeation experiments with sweep gases, desorbing and adsorbing molecules will feel the same resistance to transport into or out of the zeolite.

In Figure 15 we show the mean value of $t_{ads}$ for our dilute and dense systems as a function of temperature. For the reasons discussed above, we do not show the mean times for the dense system below $T_c$ in the figure. From the figure, it is clear that the mean time is nearly insensitive to pressure at all temperatures and shows a weak temperature dependence. The effect of temperature on the mean shows that entry into the zeolite is an activated process related to surface diffusion. The insensitivity to pressure implies that identical surface barriers exist on both sides of membranes in permeation simulations and experiments. Also shown in the figure are representative points for isobutane molecules entering the zeolite. It is an interesting and unexpected result that the mean time is nearly identical for butane and isobutane. The implication is that surface diffusion processes are more closely related to gas diffusion (which should be similar for butane and isobutane) than to diffusion inside the zeolite.
The pressures in the upstream and downstream gas phases were calculated from the gas-phase densities. On the low-pressure side, divided by the membrane area and the duration of the run. Once all of these quantities stopped changing from one run to the next, steady-state was assumed to have been reached, and the results from the final run were used. The time required to reach steady-state ranged from 10 to 100 ns.

The pressures in the upstream and downstream gas phases were calculated from the gas-phase densities. On the low-pressure side, this was done using the ideal gas law. On the high-pressure side, we used pressure-volume isotherms obtained by direct isobaric-isothermal MC simulation of the bulk gas. The permeability \( \Pi \) was calculated using the following equation

\[
\Pi = \frac{J}{\Delta P/L}
\]

where \( J \) is the flux rate of molecules across the membrane, \( \Delta P \) is the difference between the upstream and downstream gas pressures, and \( L \) is the membrane thickness (40 Å). In all cases, the downstream pressure was much smaller than the upstream pressure, so the pressure-drop and upstream pressure were almost equal in magnitude. The variation of butane and isobutane permeability with pressure-drop and temperature is shown in Figure 18. In all cases, we see the same general behavior. For low pressure drops, the permeability is independent of the pressure. As the pressure drop increases, the permeabilities start to decrease strongly. Both of these behaviors are correctly captured by the simple permeation model based on the Langmuir isotherm. The constant permeability at low pressure corresponds to the Henry’s law regime, where loading increases linearly with pressure. At sufficiently high pressures, excluded volume interactions cause the isotherm to flatten out, resulting in a monotonically decreasing permeability.

As a comparison, we also show in Figure 18 the theoretical permeabilities as a function of pressure for butane and isobutane at the simulation temperatures. Following Burggraaf,\textsuperscript{55} we have calculated the permeability based on our Langmuir isotherm fits from section IIIA, and diffusivities from section IIIB. The theoretical flux is given as

\[
J = \frac{q_{is}}{L} D_c \ln \left( \frac{1 + KP_f}{1 + KP_m} \right)
\]

Figure 17. Differences in angular distributions as a function of temperature for butane molecules in the adsorption layer of the dilute and dense systems. Excess at 500 K (200 K) is shown as a positive (negative) peak. As the temperature changes from 500 to 200 K, molecules in the dilute (dense) system tend to lie on (stick up from) the surface.

Figure 18. Permeability of butane and isobutane through a silicalite membrane as a function of pressure drop and temperature. Butane and isobutane are shown as open and closed figures, respectively, whereas the circles and squares represent 500 and 400 K, respectively. Also shown are the theoretical permeabilities for butane at 500 K (dashed line) and isobutane at 400 K (dotted line).
Figure 19. Density profiles for butane permeating across a silicalite membrane with pressure-drops of 20 300 and 491 kPa at $T = 500$ K.

Figure 20. Density profiles for isobutane permeating across a silicalite membrane with pressure-drops of 22 400 and 535 kPa at $T = 500$ K.

One reason for this underprediction can be inferred from the density profiles obtained from the simulations. For example, Figure 19 shows the profiles for butane at 500 K for both high and low pressure drops. Each membrane exhibits four density peaks corresponding to the sinusoidal channels of the zeolite, as discussed in section IVB. The outer peaks are slightly lower than inner peaks due to the lower number of zeolite atoms interacting with the butane molecules that are near the surface. What is striking about the profile is the perfect symmetry within each membrane, i.e., there is no concentration gradient. This indicates that the molecules within the zeolite are at equilibrium. This implies that the flux rate is limited by processes other than diffusion through the interior of the zeolite. The limiting processes are likely dominated by the transition from the adsorption layer to the zeolite on the upstream surface and from the zeolite to the adsorption layer on the downstream surface. The same absence of gradient is seen in all the butane runs.

Figure 20 shows the corresponding profiles for isobutane. In this case, we do see the formation of a concentration gradient in the direction of flow, and this is also true for the other isobutane simulations. It appears that switching from butane to isobutane results in a decrease in the relative importance of the surface resistance. This is understandable, given our results above. In section IVB, we showed that the mean time spent in the adsorption layer by butane and isobutane are identical, implying identical surface barriers. The diffusivity of isobutane inside the zeolite, however, is lower than that of butane by an order of magnitude. This is the same difference seen in Figure 18, implying that the permeation of isobutane is controlled by diffusion within the zeolite itself.

The absence of internal density gradients has also been observed by Pohl and Heffelfinger,58 and more recently by Nitta et al.59 The presence of surface barriers could be viewed as an anomaly associated with the extremely thin membrane sample which we have used. In fact, it could explain why our permeability predictions lie far below the experimental range. One might expect that as the membrane thickness is increased, surface effects will become negligible. However, it is not clear if this is true for the zeolite particles used in typical membranes.

VI. Conclusions

We have presented the results of molecular dynamics simulations of interfaces between single component gases of butane and isobutane and silicalite. After verifying that our potential parameters give accurate results for the experimentally measured bulk adsorption and diffusion, we investigated the dynamics of exchange between the gas and the zeolite. In particular, we have found that molecules from the gas enter the zeolite primarily via the adsorption layer, where they hop among preferred adsorption sites until entering a pore mouth. Molecules desorbing from the zeolite undergo a similar process in reverse. For both processes, $t_{ads}$ is found to be on the order of 10 ps, and is unchanged over a wide range of gas pressures, and only weakly affected by system temperature. This surface residence time is the microscopic origin of transport resistance and is present at both the feed and permeate sides of membrane permeation experiments and simulations. However, the average surface residence times are too small in comparison to bulk transit times (approximately 20 ps per unit cell) to account for the differences between macroscopic and microscopic diffusivity studies. We have simulated the permeation of butane and isobutane through thin silicalite membranes and found significant differences between our results and theoretical permeations based on Langmuir isotherms and bulk diffusion. The most likely cause of the discrepancy is the microscopic barrier, which can be significant for thin membranes.

Future work will investigate the preferential adsorption of binary gas mixtures and its role in separations processes.

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References and Notes

(34) Molecular Simulations Inc., San Diego, CA.
(45) Chandross, M.; Webb, E. B., III.; Grest, G. S., to be published.
(53) We note that the data shown in Figure 12 are all for simulations with a Langevin thermostat. We have duplicated the simulations with a Nose-Hoover thermostat, and find that we can still fit the distributions to a binomial, but with slightly different mean values and, thus, different mean times spent in the adsorption layer.
(54) The true boundary between the gas region and the adsorption layer is open to interpretation, but as long as the bulk of the peaks seen in Figure 10 are included, the results should not change greatly.
(55) We note that the data shown in Figure 12 are all for simulations with a Langevin thermostat. We have duplicated the simulations with a Nose-Hoover thermostat, and find that we can still fit the distributions to a binomial, but with slightly different mean values and, thus, different mean times spent in the adsorption layer.